CHAPTER 1

High-performance soft wearable robots for human augmentation and gait rehabilitation

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1.1 Introduction

Recent years have seen the development of an increasing number of powered exoskeletal devices for a widening range of applications. Several designs have been proposed either to enhance strength and endurance capabilities in able-bodied subjects [1] or to assist impaired movements in disabled people [2–4].

From a design perspective, wearable robots can be generally classified as rigid or soft in terms of actuation and transmission. Although rigid exoskeletons allow provision of the strongest assistance, on the other hand it is recognized that excessive mass and high impedance represent two key drawbacks of such robots [5]. In the course of addressing this issue, several designs of soft exoskeletons using pneumatics have been proposed [6]. However, pneumatic actuation typically relies on tethered air compressors, making its application for portable systems still challenging. Therefore lately soft cable-driven textile exosuits have become the new trend in wearable robots research [7]. Some examples include exosuits for ankle [8] and hip [2] joint assistance during walking. Thanks to their conformal and compliant structure, these devices are unobtrusive and extremely lightweight, but the absence of rigid links makes their design significantly challenging. The main issues are related to the difficulty of a fixed
positioning, especially corresponding to certain joints (e.g., knee), and to the unavoidable presence of shear forces that usually result in annoyance for the wearer.

Therefore trying to fill the gap between rigid exoskeletons and soft exosuits, hybrid solutions enable excellent compromises in terms of light weight, compliance, applied forces, and allowable range of motion. Remarkable performance is made possible thanks to the employment of a new actuation paradigm, purposely designed for highly dynamic interactive tasks. It constitutes a step forward toward the development of “physically intelligent” robots and will reveal opportunities for effective human–robot interaction.

The rest of the chapter will discuss how this new actuation paradigm allows dynamic interactive tasks when it is employed to power wearable robots. In Section 1.2 the involved actuation technologies are described, while Section 1.3 presents their application to three kinds of exoskeletons, for hip, knee, and back assistance. Finally, conclusions are discussed in Section 1.4.

1.2 Actuation technologies for physical human–robot interaction

Safe and dynamic interaction with humans is of paramount importance for collaborative robots. Recent exoskeletons have focused on advanced algorithms to improve control performance [2,9–13], while there is limited work in actuation hardware design.

Yet, observations from nature have highlighted that body properties of biological organisms have a key function in providing “physical intelligence” during dynamic interactive tasks. In the same manner, mechanical design of robots’ hardware represents an opportunity to provide embedded intelligence, that is, a sort of intelligence intrinsic to the system without relying on complicated control algorithms [14].

When dealing with wearable robots, indeed actuators play the greatest role among the various mechanical components.

Besides actuator prototypes for soft material robots, state–of–the–art wearable robots include three primary actuation methods, namely, conventional geared actuation, series elastic actuation (SEA), and quasi–direct drive actuation (QDD, also known as proprioceptive actuation) [14–16]. Some significant examples are reported in Fig. 1.1.
Conventional actuation uses high-speed and low-torque motors (typically brushless direct current motors, BLDC) coupled to high gear ratio transmission. It can meet the typical requirements related to assistive torque, angular velocity, and control bandwidth, but suffers from high mechanical impedance, which makes the overall system quite resistant to free movements of the wearer. Although control algorithms might be able to partially compensate for the undesirable impedance, a complete suppression of the obtrusive effects due to the high inertia of the actuator remains challenging.

Series elastic actuators (including parallel elastic actuators and other variable stiffness elastic actuators) overcome the low-compliance limitation using spring-type elastic elements. However, this solution is detrimental to the system simplicity, weight, and size, and leads to a sacrifice of the performance in control bandwidth, resulting in limited practical benefits for wearable robots.

QDD actuation instead involves a change of perspective. Being composed of high-torque motors and low gear ratio transmission, it exhibits intrinsic high torque density, high bandwidth, and high backdrivability, meeting all the multifaceted requirements of versatile wearable robots. Therefore these features identify QDD actuation as a promising technology for dynamic human–robot interaction, whose feasibility has already been proven in several preliminary tethered exoskeletons. Other recent results are reported in Section 1.3 about wearable robots for hip, knee, and back assistance.

<table>
<thead>
<tr>
<th>Actuation paradigm</th>
<th>Conventional actuation</th>
<th>Series elastic actuation</th>
<th>Conventional actuation and textile wearable</th>
<th>Quasi direct drive actuation</th>
</tr>
</thead>
<tbody>
<tr>
<td>Torque (Nm)</td>
<td>70 ▶️</td>
<td>60 ▶️</td>
<td>32 ▶️</td>
<td>48 ▶️</td>
</tr>
<tr>
<td>Mass (kg)</td>
<td>23 ▼</td>
<td>7 ▼</td>
<td>5 ▼</td>
<td>3 ▼</td>
</tr>
<tr>
<td>Bandwidth (Hz)</td>
<td>5 ▼</td>
<td>7 ▼</td>
<td>20 ▶️</td>
<td>44 ▶️</td>
</tr>
<tr>
<td>Compliance (Nm)</td>
<td>30 ▼</td>
<td>9 ▼</td>
<td>N/A ▼</td>
<td>0.4 ▶️</td>
</tr>
<tr>
<td>Torque density (Nm/kg)</td>
<td>3 ▼</td>
<td>8.6 ▼</td>
<td>6.4 ▼</td>
<td>16 ▶️</td>
</tr>
</tbody>
</table>

Figure 1.1 Performance comparison of selected exemplifying embodiments of the main actuation methods employed in wearable robots [14]. They include conventional geared actuators, in both rigid [17] and textile exosuits [9,18], series elastic actuators [19,20], and quasi-direct drive actuators [15].
1.2.1 High torque density motors

QDD actuation is a new paradigm of robot actuation design that leverages high torque density motors with low ratio transmission mechanism [14,28]. It has been recently studied for legged robots [14] and exoskeletons [29].

The benefits of high torque density actuation include a simplified mechanical structure with reduced mass and volume, and high compliance, that is, high backdrivability. Thus it is an ideal candidate to satisfy static and dynamic requirements of wearable robots.

A crucial component for the design of high torque density actuation is the high torque density motor. In [30] a custom BLDC motor is designed with optimized mechanical structure, topology, and electromagnetic properties. It uses high-temperature resistive magnetic materials and adopts an outer rotor and a flat, concentrated winding structure to maximize the torque density [31,32]. As shown in Fig. 1.2A, in order to enhance the efficiency the motor uses fractional-slot type winding, which allows it to reduce the cogging torque and to minimize the copper loss. It has 21 pole pairs and 36 rotor

![Figure 1.2](image)

Figure 1.2 (A) Design of custom brushless DC electric motor (BLDC) with exterior rotor and concentrated winding. The fractional-slot design (36 slots, 21 pole pairs) allows it to reduce cogging torque and to minimize copper loss [33]. (B) Finite element analysis shows that by using sintered neodymium iron boron permanent magnets the magnetic strength of the stator can reach 1.9 T, under condition of no current in the winding. (C) Distribution of continuous torque density versus air gap radius for our custom motor compared to commercial ones. It is worth noting that exoskeletons typically need motors with air gap radius in the 35–40 mm range. Thanks to its ad hoc design, the custom motor developed at The City University of New York, marked with a star in the plot, exhibits continuous torque density (7.81 Nm/kg) 10.4 times higher than the Maxon brushless DC motor EC flat 90 (#323772, 0.75 Nm/kg), widely used in the exoskeleton industry.
slots, a number significantly higher than the 12 pole pairs of the commercial motor Maxon EC90 [23] or the 10 pole pairs and 18 rotor slots of another concurrent research prototype [33]. Moreover, unlike conventional BLDC motors that place windings around the rotor, here motor winding is attached to the stators and the rotor consists only of the cover and 1-mm-thick permanent magnet chips. In this way, the lightweight exterior rotor reduces rotary inertia and increases the torque to inertia ratio. Finally, a further detail not to be neglected involves the choice of the electromagnetic material: permanent magnets are made of sintered neodymium iron boron (NdFeB), which can reach 1.9 T magnetic field intensity, as shown by finite element analysis reported in Fig. 1.2B.

Overall, this design allows a significant reduction in the inertia and mechanical impedance of the motor while increasing its control bandwidth. It weighs 256 g and provides 2 Nm continuous torque. Fig. 1.2C shows the distribution of continuous torque density versus air gap radius for this motor compared to commercial ones [28]. In the 35–40 mm air gap radius domain, usually adopted for wearable robots, the continuous torque density of the described motor is 7.81 Nm/kg, remarkably higher than the values of the widely used T-motor U8 (3.5 Nm/kg) and Maxon EC Flat 90 (#323772, 0.75 Nm/kg).

1.2.2 Quasi-direct drive actuation

The high torque density motor constitutes an important step toward an effective actuation strategy for wearable robots. To keep the system compact and lightweight, it is worth combining the motor with all the related components in a fully integrated actuator, as shown in Fig. 1.3A [34,35].

The overall actuator weight is 777 g and it includes the high torque density motor, an 8:1 ratio planetary gear, a 14-bit high accuracy magnetic encoder, and a wide range input (10–60 V) motor driver and controller.

Detailed specifications of the resulting actuator can be found in Table 1.1, together with the corresponding values of a reference example from conventional actuators and series elastic actuators.

Low-level control on position, velocity, and current is implemented in the driver-control electronics, whereas real-time information for high-level control transfer is through the Controller Area Network (CAN bus) communication protocol.

When powered with a nominal voltage of 42 V, the actuator reaches a nominal speed of 188 RPM (19.7 rad/s). Moreover, thanks to the quasi-
direct drive strategy using low gear ratio transmission, the actuator presents low output inertia (57.6 kg·cm²), which means low resistance to natural human movements.

Regarding the output capability, it is worth noting that it is highly limited by the motor’s winding temperature. To evaluate the actuator working current performance, it was operated continuously in stall mode under different output currents. The stator temperature was measured by an embedded temperature sensor and the surface temperature was measured by a portable FLIR thermal camera. The experiment was performed in a 22°C lab environment without external heat dissipation. The maximum operating time was set to 15 min and the maximum temperature of the stator to 100°C. In Fig. 1.3B the evolution over time of the stator temperature is plotted for different current conditions, while Fig. 1.3C shows the thermal camera image of the actuator surface after 15 min.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Unit</th>
<th>Conventional [21]</th>
<th>SEA [23]</th>
<th>QDD</th>
</tr>
</thead>
<tbody>
<tr>
<td>Output rated torque</td>
<td>Nm</td>
<td>8</td>
<td>40</td>
<td>17.5</td>
</tr>
<tr>
<td>Actuator mass</td>
<td>kg</td>
<td>~0.50</td>
<td>1.80</td>
<td>0.77</td>
</tr>
<tr>
<td>Actuator rated torque</td>
<td>Nm/kg</td>
<td>16</td>
<td>22.2</td>
<td>20.7</td>
</tr>
<tr>
<td>density</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Control bandwidth</td>
<td>Hz</td>
<td>5.1</td>
<td>4.2</td>
<td>73.3</td>
</tr>
<tr>
<td>Backdrive torque</td>
<td>Nm</td>
<td>—</td>
<td>—</td>
<td>0.97</td>
</tr>
</tbody>
</table>
under 7.5 A nominal current, demonstrating that a highest temperature of 62.7°C is reached. This experiment validates that the actuator can produce a continuous output torque of 17.5 Nm under 7.5 A rated current.

1.3 Applications to wearable robots

Having discussed the properties of QDD actuation and its potential impact on applications involving dynamic human—robot interaction, this section will analyze in detail three different use cases: a portable exoskeleton for hip assistance during walking and squatting, and two tethered versions, one for knee support during squatting and the other for back assistance in stoop lifting.

1.3.1 Hip exoskeleton

During walking human hip joints have flexion/extension movements in the sagittal plane and abduction/adduction movements in the frontal plane. Therefore a hip exoskeleton needs to accommodate those two degrees of freedom. For level-ground walking, the range of motion of a human hip joint is 32.2 degrees flexion, 22.5 degrees extension, 7.9 degrees abduction, and adduction 6.4 degrees [36]. Here the robot is designed with a larger range of motion than the standard requirements to handle a heterogeneous population for a wide variety of activities beyond walking, such as squatting, sitting, and stair climbing. Moreover, it was observed that for a human of 75 kg walking at 1.25 m/s the peak torque and the speed of the hip joint are 97 Nm and 3.5 rad/s, respectively, but results in [37] and [38] show that a 12 Nm torque assistance is sufficient to produce a 15.5% reduction in metabolic cost for uphill walking.

1.3.1.1 Design

The mechanical system of the hip exoskeleton is symmetric about the sagittal plane and is mainly composed of a waist frame, two actuators, two torque sensors, and two thigh braces, as shown in Fig. 1.4. The waist frame has the main function of anchoring the actuators. It has a curvature conformal to the wearer’s pelvis, enabling uniform force distribution on the human body. A wide waist belt is used to attach the waist frame to the user, aiming at maximizing the contact area so as to reduce the pressure on the human. The motor housings are connected to the waist frame by means of hinge joints that enable passive degrees of freedom in the frontal plane (e.g., abduction and adduction), whereas the actuators work in the sagittal plane to assist the flexion and extension of the hip joints. A
customized compact torque sensor is assembled to the output flange of the actuator to measure the output torque. Finally, the thigh brace is fixed to the sensor and transmits the actuator torque to the wearer’s thigh thanks to a fastening strap. In order to alleviate the wearer from painful shear forces, the thigh brace has a curved structure that enables it to provide assistive forces on the thigh perpendicularly to the frontal plane. Regarding the electrical system, it supports high-level torque control, low-level motor control, sensor signal conditioning, data communication, and power management. The local motor controller is developed based on a motor driver and a DSP microcontroller. It allows measurement of the motor motion status and to realize control based on current, velocity and position. The high-level microcontroller runs on Arduino Due and performs torque control. It acquires real-time data on the lower-limb posture from the wireless inertial measurement unit (IMU) sensors and on the applied torques from the loadcells.

### 1.3.1.2 Modeling

The overall system can be broken down into four main subsystems, as shown in Fig. 1.5: the motor, the transmission mechanism, the wearable structure, and the human leg. Connections between these modules are represented as springs and dampers to model the force and motion transmission.
The dynamics of the motor electrical system can be characterized by the winding resistance $R$ and inductance $L$. Subject to input voltage $V$, the motor generates a torque $\tau_m$ proportional to the current $i$ and to the torque constant $k_t$, whereas the back-electromagnetic force $V_b$ is proportional to the motor velocity $\dot{\theta}_m$ and to the constant $k_b$. Therefore the governing equations of the motor electrical system are

\begin{align}
V - V_b &= L \frac{di}{dt} + Ri \\
\tau_m &= k_t i \\
V_b &= k_b \dot{\theta}_m
\end{align}

Meanwhile, from a mechanical perspective the motor is described by the equation

\[ \tau_m = J_m \ddot{\theta}_m + b_m \dot{\theta}_m + \tau_1 \]

where $J_m$ denotes the moment of inertia of the rotor around its rotation axis, $b_m$ is the damping coefficient that takes into account internal viscous friction, $\theta_m$ denotes the motor angle, and $\tau_1$ is the torque applied to the output shaft.

Then, considering a gearbox with gear ratio $n:1$, it has the effect of reducing the angular velocity and amplifying the torque according to the equations

\[ \theta_1 = \theta_m; \quad \theta_2 = \frac{\theta_1}{n}; \quad \tau_2 = n \tau_1. \]

In Eq. (1.5), $\theta_1$ and $\theta_2$ denote the rotation angles of the input and output shafts of the gearbox, respectively, and $\tau_1$ and $\tau_2$ the corresponding applied torques.
The wearable structure of the exoskeleton can be designed with rigid linkages, springs, cable—pulley systems, and cable—textile systems. In all the cases, it can be modeled through global parameters, namely stiffness $k_c$ and damping $b_c$. Therefore the resulting equation for the dynamics of the wearable structure is

$$\tau_2 = b_c (\dot{\theta}_2 - \dot{\theta}_h) + k_c (\theta_2 - \theta_h).$$

(1.6)

Finally, the human limb is governed by the equation

$$J_t \ddot{\theta}_h + b_c (\dot{\theta}_h - \dot{\theta}_2) + k_c (\theta_h - \theta_2) = \tau_l,$$

(1.7)

where $J_t$ is the inertia of the limb with the orthosis, $\theta_h$ is the hip rotation angle, $\tau_l$ is the human torque generated by the muscles, and $\tau_a$ is the torque applied on the human thigh. $\tau_a$ can be an assistive or resistive torque and can be calculated as

$$\tau_a = \tau_2 = b_c \left( \frac{\dot{\theta}_m}{n} - \dot{\theta}_h \right) + k_c \left( \frac{\theta_m}{n} - \theta_h \right).$$

(1.8)

Assume as initial condition $\theta_h(0)$, $\dot{\theta}_h(0)$, and $V(0)$ equal to zero and neglect the inductance $L$ due to its small value [39]. Let $s$ be the Laplace variable, in the $s$-domain the assistive torque $\tau_a(s)$ is related to the hip rotation angle $\theta_h(s)$ and input voltage $V(s)$ as expressed in Eq. (1.9).

$$\tau_a(s) = G_1(s)V(s) + G_2(s)\theta_h(s) = n_1(s) \left[ \frac{n_2(s)}{d(s)} V(s) + \frac{n_3(s)}{d(s)} \theta_h(s) \right],$$

(1.9)

where

$$n_1(s) = (b_c s + k_c)$$

$$n_2(s) = nk_t$$

$$n_3(s) = -n^2 \left[ J_m R \dot{s}^2 + (Rb_m + k_bk_t)s \right]$$

(1.10)

$$d(s) = J_e s^2 + b_c s + k_c$$

$$J_e = n^2 J_m R; b_e = n^2 Rb_m + n^2 k_bk_t + Rb_c; k_e = Rk_c.$$
The natural frequency $\omega_n$ of the open-loop torque control for the second-order system is

$$\omega_n = \sqrt{\frac{k_c}{J_c}} = \sqrt{\frac{Rk_c}{n^2 J_m R}} = \frac{k_c}{n^2 J_m}. \quad (1.11)$$

The effective moment of inertia $J_e$ is equal to $n^2 J_m$, hence the natural frequency $\omega_n$ of the open-loop torque control is directly proportional to wearable structure stiffness $k_c$ and inversely proportional to the square of the gear ratio $n$ and the moment of inertia of the motor $J_m$.

The described model allows also to make some considerations about the backdrivability. To identify the property of the passive mechanism, $V(s)$ is set to zero and the output resistive torque $\tau_a$ induced by the human motion $\theta_h(s)$ can be derived from Eq. (1.12), while Eq. (1.13) provides the output link impedance.

$$\tau_a(s) = G_2(s)\theta_h(s) = \frac{-(b_c s + k_c) - J_m R s^2 + (R b_m + k_b k_i) s}{n^2 J_m R s^2 + (R b_m + k_b k_i) s + R b_c} \theta_h(s) \quad (1.12)$$

$$Z_o(s) = \frac{\tau_a(s)}{s \theta_h(s)} \quad (1.13)$$

As the gear ratio is sufficiently small, the resistive torque can be neglected, because

$$\lim_{n \to 0} \tau_a(s) = 0 \quad (1.14)$$

As the gear ratio is large enough, the resistive torque is approximated by Eq. (1.15), where the wearable structure damping $b_c$ and stiffness $k_c$ are the dominating terms.

$$\lim_{n \to \infty} \tau_a(s) \approx -(b_c s + k_c) \theta_h(s) \quad (1.15)$$

When the gear ratio is equal to 1, the resistive torque is expressed by Eq. (1.16). It depends on the gear ratio $n$, the damping term $b_c$, the stiffness $k_c$, the motor inertia $J_m$, the motor damping $b_m$, the motor resistance $R$, the motor torque constant $k_t$, and the back EMF constant $k_b$.

$$\tau_a(s)|_{n=1} = \frac{(b_c s + k_c)(J_m R s^2 + R b_m s + k_b k_i s + R b_c) \theta_h(s)}{J_m R s^2 + (R b_m + k_b k_i + R b_c) s + R k_c} \quad (1.16)$$
Therefore from Eqs. (1.14), (1.15), and (1.16) it is clear that high backdrivability (i.e., low resistive torque and low output impedance) can be achieved with small gear ratio $n$, small damping constant $b_c$, and small stiffness $k_c$.

### 1.3.1.3 Control

The control system is based on a hierarchical architecture composed of a high-level control layer that robustly detects gait intention (Fig. 1.6 top), a middle-level control that generates the assistive torque profile (Fig. 1.6 bottom), and a low-level control layer that implements a current-based torque control.

An algorithm based on a data-driven method [40] with a neural network regressor is used to compensate for the uncertainties caused by changing gait speeds. It estimates the walking and squatting cycle percentage in real-time by the signals from two IMUs mounted on the anterior of both thighs (Fig. 1.4). These sensors provide motion information, including Euler angles, angular velocities, and accelerations at a frequency of 200 Hz. Motion information during the last 0.4 s sliding time window constitutes the input vector of the neural network for both offline training process and online control. The neural network used in this algorithm has one hidden layer with 30 neurons as well as a sigmoid activation function and deploys the Xavier initialization [41] for the network weights.

![Figure 1.6](image)

**Figure 1.6** (Top) Estimated gait cycle percentage accurately matches the ground truth. The latter is calculated offline by insole signals, while the estimation is provided applying a regression method to information from IMUs. The robust gait recognition ($R^2 = 0.997$) is able to compensate for the disturbances due to walking speed changes. (Bottom) Assistive torque profile generated by the control algorithm.
algorithm could achieve an $R^2 = 0.997$ on a test set of walking and squatting data collected from three able-bodied subjects at several different speeds.

After obtaining the gait percentage, the middle-level controller calculates the assistive torque proportionally according to a predefined torque profile expressed as a look-up table. Basically, the desired assistive torque is obtained by searching the gait percentage in the look-up table and using interpolation to fill in the missing data. The predefined torque profile for walking is generated by the human biological model in [42], while the one for squatting is expressed as a simple sine wave.

Finally, the low-level torque control architecture is composed of an inner and an outer loop control. The inner loop implements motor current control in the local motor controller, while the outer loop performs torque control in Arduino Due using feedback signals from motors, load-cells, and IMU-based gait recognition.

1.3.1.4 Evaluation

Several experiments were conducted on the hip exoskeleton to characterize its mechanical versatility through backdrivability and bandwidth demonstrations.

For the bandwidth experiment chirp signals with different magnitudes were used as reference torque to obtain the Bode plot. Results are shown in Fig. 1.7A, where bandwidth values of 57.8, 59.3, and 62.4 Hz are obtained for 10, 15, and 20 Nm chirp magnitude, respectively. Thus the bandwidth is much higher than the requirement of human walking, but this property turns out to be useful for agile human activities, for example, running and balance control to unexpected external disturbance. Compared with the exoskeleton using SEA [19], characterized by 5 Hz bandwidth, a high control bandwidth robot is safer and more robust to uncertainties.

For the backdrivability experiment, instead, the backdrive torque was measured in unpowered mode. An angular displacement of 32.2 degrees was imposed to the hip joint at 1 Hz frequency while the actuator was turned off and the resistance torque was measured. The profiles of the rotation angle and the backdrive torque are reported in Fig. 1.7B. Results show that the hip exoskeleton presents a very low backdrive torque (maximum value is about 0.4 Nm), demonstrating higher compliance than other state-of-the-art exoskeletons [19,33].
As a last experiment, a control test was performed to investigate the torque tracking performance of the hip exoskeleton. It was tested during treadmill walking with varying speed from 0.8 to 1.4 m/s and during squatting with 2 s cadence. A total of 15 tests with the same torque profile were performed for each of the walking and squatting motions. The tracking performance of the hip assistance is shown in Fig. 1.7C. The average root mean square error (RMSE) between the desired and actual torque trajectory in 60 tests is 1.09 Nm (5.4% of the maximum desired torque). This result indicates that the torque controller is able to track with high accuracy the desired assistance during walking and squatting.

1.3.2 Knee exoskeleton

Recently there is a growing interest in wearable robots for knee joint assistance as cumulative knee disorders account for 65% of lower
extremity musculoskeletal disorders. Squatting and kneeling are two of the primary risk factors that contribute to knee disorders [43].

Knee joint assistance during squatting necessitates a broad range of motion (0–130 degrees flexion) and joint torque (up to 60 Nm) [44]. Moreover, for an effective synchronization with the wearer, the torque generated from the robot needs to be delivered at an angular velocity of no less than 2.4 rad/s.

1.3.2.1 Design
Most of the existing knee exoskeletons are designed for walking assistance [45,46] and they typically do not allow the squat motion due to the interference between the robot structure and human bodies (e.g., [47,48]). Since the focus of the work is to understand the feasibility of the approach for squat assistance, the exoskeleton consists of a wearable robot emulator, that is a tethered wearable structure with offboard actuation. Fig. 1.8A shows the overall system, including the wearable structure, a bidirectional Bowden cable transmission mechanism and the high torque density actuator implemented as a tethered platform. It is worth noting that though the current platform is configured as a tethered system, it can be easily converted to a portable system, as the overall mass of motor and gears is 0.55 kg.

The bidirectional Bowden cable mechanism (similar to [49] and [50]) uses a single motor to generate bidirectional actuation, that is, knee flexion and extension. In this regard, a key role is played by the knee joint mechanism (Fig. 1.8B), that constitutes the distal portion of the bidirectional cable-drive mechanism. It is designed to be lightweight and low-profile, namely to avoid interference with the human body during squat motion.

The assembly includes one flexion cable and one extension cable that pass around the distal pulley and terminate at the cable locking mechanism. One side of the knee mechanism is attached to the thigh brace while the shank plate is fixed to the calf brace. A load cell connects the thigh and the calf links and plays a key role in force transmission between the cable and the shank plates. In fact, when the cable is pulled, it actuates the pulley through the locking mechanism and drives the shank plate via the loadcell.

The exoskeleton is attached to the body via 3D printed carbon fiber braces designed to be conformal to the human leg. Thanks to these braces the torque at the knee joint is converted into pressure distributed along the length of the thigh and the shank. Therefore the size of the wearable arms
plays a crucial role in the performance and user comfort. Three-dimensional infrared scans (Sense 2, MatterHackers Inc.) of the wearer’s leg are taken and processed into a CAD model. This model is then 3D printed using fused deposition modeling with carbon fiber reinforcements. Foam padding is also added in the locations of leg contact to aid in comfort, while Velcro straps are used to anchor the exoskeleton arms to the leg.

1.3.2.2 Modeling
A human biomechanics model is derived to calculate the knee joint torque to assist both squat and stoop lifting activities in real time. Unlike

Figure 1.8 (A) The hip exoskeleton includes the wearable structure with the knee joint mechanism, a bidirectional Bowden cable transmission system, and a high torque density actuation platform. (B) Section view (left) and isometric view (right) of the cable-driven knee joint mechanism for bidirectional actuation, that is, knee flexion and extension.
methods that use simple and predefined profiles (e.g., sine waves) to approximate the human joint torque, this method is biologically meaningful and applicable to squat, stoop, and walking activities. In [51] an assistive algorithm for a squat assistance exoskeleton is proposed assuming that the back of the subject is straight, and the trunk angle is zero. It only uses knee joint angle to calculate the required torque and lacks the posture information of the hip and trunk. However, during lifting (squat and stoop) the back angle varies and significantly affects the knee joint torque.

Since squat and stoop involve significantly different biomechanics of the knee joint, this model is versatile in the sense that it can cover both scenarios for a wide variety of people. The knee joint torque $\hat{\tau}_k$ can be derived from Eq. (1.17)

$$\hat{\tau}_k = I(\theta)\ddot{\theta} + C(\theta, \dot{\theta})\dot{\theta} + G(\theta),$$

where $\theta$ is the joint angles, $I(\theta)$ is the inertia matrix, $C(\theta, \dot{\theta})$ denotes the centrifugal and Coriolis term, and $G(\theta)$ is the gravitational loading.

As typically lifting tasks are relatively slow, the knee joint torque is dominated by the gravitational loading. Thus, with reference to Fig. 1.9, estimated knee joint torque $\hat{\tau}_k$ can be computed using a quasi-static model, as expressed in Eq. (1.18).

$$\hat{\tau}_k = G(\theta) = -0.5[M_g g (L_b \sin \theta_b + L_t \sin \theta_t) + M_g g L_e \sin \theta_e]$$

Here the knee extension is defined as the positive direction for the knee joint torque $\hat{\tau}_k$, while the clockwise direction is defined as the positive direction for the trunk angle $\theta_b$, the thigh angle $\theta_t$, and the shank

![Figure 1.9](image.jpg) Quasi-static model used to derive the assistive knee joint torque during squat motion.
angle $\theta_s$. $M_b$ is the combined mass of the head, neck, thorax, abdomen, pelvis, arms, forearms, and hands, $M_i$ is the mass of thigh, $L_b$ is the length between the center of mass $M_b$ and the hip pivot, $L_t$ is the length of thigh between the hip and the knee pivots, $L_{tc}$ is the length between the center of mass $M_t$ and the knee pivot, and $g$ is the gravitational constant. The parameters $L_b$, $L_t$, $L_{tc}$, $M_b$, $M_t$ are calculated according to Eqs. (1.19–1.23) using data in Table 1.2 obtained from anthropometry research [52]. It is worth noting that the proposed model is customizable to different individuals because the assistive torque can be adjusted to the subject’s weight and height by means of the weight ratio (ratio between the subject weight $M_{sb}$ and the human model weight $M_W$) and the height ratio (ratio between the subject height $L_{sb}$ and the human model height $L_H$).

\begin{align*}
M_b &= \left( \frac{M_{sb}}{M_W} \right) \cdot \sum_{i=1}^{8} M_i \\
M_t &= \left( \frac{M_{tb}}{M_W} \right) \cdot M_9
\end{align*}

(1.19)

(1.20)

**Table 1.2** The human segment parameters.

<table>
<thead>
<tr>
<th>#</th>
<th>Segment</th>
<th>$M_i$: Mass (kg)</th>
<th>$L_i$: Length between center of mass to ground (m)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Head</td>
<td>$M_1$: 4.2 kg</td>
<td>$L_{11}$: 1.679 m</td>
</tr>
<tr>
<td>2</td>
<td>Neck</td>
<td>$M_2$: 1.1 kg</td>
<td>$L_2$: 1.545 m</td>
</tr>
<tr>
<td>3</td>
<td>Thorax</td>
<td>$M_3$: 24.9 kg</td>
<td>$L_3$: 1.308 m</td>
</tr>
<tr>
<td>4</td>
<td>Abdomen</td>
<td>$M_4$: 2.4 kg</td>
<td>$L_4$: 1.099 m</td>
</tr>
<tr>
<td>5</td>
<td>Pelvis</td>
<td>$M_5$: 11.8 kg</td>
<td>$L_5$: 0.983 m</td>
</tr>
<tr>
<td>6</td>
<td>Arms</td>
<td>$M_6$: 4 kg</td>
<td>$L_6$: 1.285 m</td>
</tr>
<tr>
<td>7</td>
<td>Forearms</td>
<td>$M_7$: 2.8 kg</td>
<td>$L_7$: 1.027 m</td>
</tr>
<tr>
<td>8</td>
<td>Hands</td>
<td>$M_8$: 1 kg</td>
<td>$L_8$: 0.792 m</td>
</tr>
<tr>
<td>9</td>
<td>Thighs</td>
<td>$M_9$: 19.6 kg</td>
<td>$L_9$: 0.75 m</td>
</tr>
<tr>
<td>10</td>
<td>Calves</td>
<td>$M_{10}$: 7.6 kg</td>
<td>$L_{10}$: 0.33 m</td>
</tr>
<tr>
<td>11</td>
<td>Feet</td>
<td>$M_{11}$: 2 kg</td>
<td>$L_{11}$: 0.028 m</td>
</tr>
<tr>
<td>12</td>
<td>Hip pivot to ground</td>
<td></td>
<td>$L_{12}$: 0.946 m</td>
</tr>
<tr>
<td>13</td>
<td>Knee pivot to ground</td>
<td></td>
<td>$L_{13}$: 0.505 m</td>
</tr>
</tbody>
</table>

Total weight $M_W$: 81.4 kg  
Total height $L_H$: 1.784 m
\[ L_b = \left( \frac{L_{sb}}{L_H} \right) \cdot \left\{ \frac{8}{\sum_{i=1}^{8} (M_i \cdot L_i) - L_{12}} \right\} \] (1.21)

\[ L_d = \left( \frac{L_{sb}}{L_H} \right) \cdot (L_{12} - L_{13}) \] (1.22)

\[ L_{dc} = \left( \frac{L_{sb}}{L_H} \right) \cdot (L_{9} - L_{13}) \] (1.23)

Finally, given the estimated joint torque \( \hat{\tau}_k \), the desired assistive torque \( \tau_r \) to be provided by the exoskeleton is defined as

\[ \tau_r = \alpha \cdot \hat{\tau}_k. \] (1.24)

As long as the gain \( \alpha \) is positive, the exoskeleton will assist the wearer. It can be used to reduce the loading and increase the endurance of workers. On the other hand, when the gain \( \alpha \) is negative, the exoskeleton will resist the human. It can be useful to increase the muscle strength for healthy subjects in fitness activities or individuals with movement impairments in rehabilitation.

### 1.3.2.3 Control

The control system is based on a two-level configuration architecture, as shown in Fig. 1.10: a target computer is used for high-level assistive control, while local motor driver electronics perform low-level control. The control strategy follows the method adopted in [53], where the authors demonstrate accurate force tracking of a robot arm in contact with surfaces of unknown linear compliance. Here, the same strategy is adapted to control the interaction torque between exoskeleton and human. Unlike [11], where a predefined and fixed torque reference is used, the present control provides adaptive assistance to the wearer based on the biomechanics model for both squatting and stooping.

The high-level controller runs at 1 kHz and implements a torque loop proportional–integral–derivative (PID) scheme to track the reference assistive torque.
The low-level controller instead implements a velocity loop PID scheme running at 20 kHz, and a current PID control running at 200 kHz. It measures the real-time motor status (i.e., current, velocity, and position) and communicates with the target computer through the CAN bus.

In addition, three IMU sensors, and one loadcell are connected to the computer through corresponding interface boards. The IMUs provide measurements of the trunk angle $\theta_b$, thigh angle $\theta_t$, and shank angle $\theta_s$ with a sampling rate of 400 Hz.

They are calibrated to zero degrees at the beginning of the experiment, while the subject is instructed to stand straight. Then, the knee angle $\theta_k$ and hip angle $\theta_h$ are calculated by Eqs. (1.25–1.26) and their positive directions represent an extension.

$$\theta_k = \theta_t - \theta_s$$ (1.25)

$$\theta_h = \theta_t - \theta_b$$ (1.26)

### 1.3.2.4 Evaluation

Several experiments were carried out to demonstrate the compliance of the exoskeleton, the control effectiveness, and the torque tracking performance.

The study was approved by the City University of New York Institutional Review Board, and all methods were carried out in accordance with the approved study protocol. Based on the experimental
procedure, three healthy subjects performed five repetitions of squat motion. Rhythm was marked by a metronome and each cycle took 8 s, as shown in Fig. 1.11.

Figure 1.11 Squat assistance control strategy. Top graph plots the evolution over time of the trunk, hip, thigh, knee, and shank angles during two squatting cycles. Bottom graph reports the required knee joint torque, and both the desired and actual assistive torques in the case of 50% level of assistance.
For the compliance evaluation, the backdrive torque was measured during squatting in unpowered condition. Thanks to the high torque density motor, the low gear ratio transmission, and low-friction cable-drive mechanism, a very low mechanical impedance is obtained, as shown in Fig. 1.12A. The peak backdrive torque is registered at the onset of motor rotation and corresponds to the changes of direction. The average resistant torque is 0.92 Nm, while its maximum value is 2.58 Nm, much lower than other state-of-the-art knee exoskeletons (for instance, as an example case the corresponding peak resistance in [29] is 8 Nm). These results were confirmed also by the subjects, who reported extremely low resistance while wearing the device.

The same test was performed also with zero torque tracking control, whereby the resistant torque was measured while the actuator was turned on and the reference torque was steadily set to zero, regardless of human motion. This trial was implemented to compensate for the mechanical resistance, such as friction of the cable and gears. Accordingly, the mechanical impedance was further reduced compared to the unpowered condition, as shown in Fig. 1.12B. The average resistant torque is 0.34 Nm (4 times lower), while its maximum value is 0.64 Nm (2.7 times lower).

As a further evaluation, the torque tracking performance during squatting was analyzed for three levels of assistance, namely 10%, 30%, and 50% of the required knee joint torque calculated by Eq. 1.18, corresponding to $\alpha = 0.1$, $\alpha = 0.3$, and $\alpha = 0.5$ in Eq. 1.24, respectively. Therefore

![Figure 1.12](image_url)

**Figure 1.12** Characterization of the mechanical impedance during squatting in the case of unpowered condition (A) and zero torque tracking control (B). The orange line indicates the knee angle, while the blue one shows the measured resistant torque. The peak backdrive torque is registered at the onset of motor rotation and corresponds to the changes of direction. Average backdrive torque is 0.92 Nm in case (A) and 0.34 in case (B), while the peak values are 2.58 and 0.64 Nm, respectively.
the assistive control was used to augment human knee joints during squats by applying specific torque depending on the current trunk angle $\theta_b$ and thigh angle $\theta_t$ detected by the IMU sensors. The tracking performance is shown in Fig. 1.13.

The RMSE between the desired and actual torque trajectory is 0.23 Nm (2.8% of 7.6 Nm peak torque), 0.22 Nm (1.1% of 20 Nm peak torque), and 0.29 Nm (1.2% of 23.9 Nm peak torque) in 10%, 30%, and 50% knee assistance, respectively. These results demonstrate that the torque controller can deliver the desired torque profile with higher accuracy: the overall RMSE of torque tracking is about 0.29 Nm (1.2% of the peak torque) while for instance in [54] it is 2.1 Nm (21% error of 10 Nm peak torque).

Finally, the effectiveness of the assistance provided by the exoskeleton was evaluated in terms of its capability to reduce muscle activity.

For this purpose, the knee extensors (rectus femoris, vastus lateralis, vastus medialis) and the knee flexors (biceps femoris and semitendinosus) EMG signals were observed in six different scenarios: without the

![Figure 1.13](image.png)

**Figure 1.13** Tracking performance of 10%, 30%, and 50% knee torque assistance in three squatting cycles. The RMSE between the desired and actual torque trajectory is 0.23, 0.22, and 0.29 Nm, respectively. Overall RMSE of torque tracking is less than 0.29 Nm (1.21% of 24 Nm peak torque).
exoskeleton, power-off exoskeleton, zero torque control assistance, 10%, 30%, and 50% assistance.

Fig. 1.14A reports the data relative to the vastus lateralis of a single subject. It shows that in the passive condition, due to the mechanical impedance of the wearable structure EMG amplitude of power-off condition is slightly higher than the one without exoskeleton. In the active condition the EMG amplitude of the zero torque control is pretty similar to the one without exoskeleton, while it is clearly reduced in 10%, 30%, and 50% assistance. Therefore these results reveal that the assistive control is effective in reducing the effort of the knee extensor muscle.

In an attempt to analyze the assistive effect in a more comprehensive way, Table 1.3 and Fig. 1.14B report the RMS amplitude of the EMG signals of the five observed muscles for each of the six conditions, whereby data are averaged over 15 squat cycles (five squat cycles per three subjects). EMG of

Figure 1.14 Muscle activities during squatting in six different conditions: without-exoskeleton, power-off, zero torque control, 10%, 30%, and 50% assistance. (A) The vastus lateralis EMG of a single subject is plotted. It reveals that the assistive control has the beneficial effect of reducing the effort of the vastus lateralis muscle. (B) EMG data of knee extensor (rectus femoris, vastus lateralis, and vastus medialis) and flexor (biceps femoris and semitendinosus) muscles during squatting in different conditions. Lines represent the average RMS EMG from 15 squat cycles (five squat cycles per three subjects). Results shows that due to exoskeleton assistance the activities of the knee extensor muscles were reduced, while those of flexor muscles were increased.
Knee extensors (rectus femoris, vastus lateralis, vastus medialis) reach the highest amplitude in power-off condition, but they are not significantly different to the cases without exoskeleton and with zero torque control. In particular, the values of standard deviation between these two conditions are 0.0188, 0.0136, and 0.0246 for rectus femoris, vastus lateralis, and vastus medialis, respectively. Meanwhile, it is clear that the higher the torque delivered to the wearer, the lower is the muscle activity of the knee extensors. However, an increase of the muscle activities of knee flexors (biceps femoris and semitendinosus) is observed. As these are bi-articular muscles, which extend the hip and flex the knee, their increased activation is possibly required to stabilize the pelvis in response to the assistance. Another reason for this effect may be found in the lack of training by the novice users of the exoskeleton. Further investigation will be needed for a precise clarification.

### Table 1.3 Average RMS EMG in knee muscles.

<table>
<thead>
<tr>
<th>Muscles</th>
<th>Sub.</th>
<th>WO</th>
<th>Off</th>
<th>0%</th>
<th>10%</th>
<th>30%</th>
<th>50%</th>
</tr>
</thead>
<tbody>
<tr>
<td>Rectus femoris</td>
<td>S1</td>
<td>78</td>
<td>87</td>
<td>35</td>
<td>25</td>
<td>28</td>
<td>11</td>
</tr>
<tr>
<td></td>
<td>S2</td>
<td>31</td>
<td>36</td>
<td>45</td>
<td>26</td>
<td>15</td>
<td>10</td>
</tr>
<tr>
<td></td>
<td>S3</td>
<td>56</td>
<td>65</td>
<td>49</td>
<td>46</td>
<td>35</td>
<td>39</td>
</tr>
<tr>
<td><strong>Avg.</strong></td>
<td></td>
<td><strong>55</strong></td>
<td><strong>62</strong></td>
<td><strong>43</strong></td>
<td><strong>32</strong></td>
<td><strong>26</strong></td>
<td><strong>20</strong></td>
</tr>
<tr>
<td>Vastus lateralis</td>
<td>S1</td>
<td>123</td>
<td>149</td>
<td>108</td>
<td>50</td>
<td>47</td>
<td>26</td>
</tr>
<tr>
<td></td>
<td>S2</td>
<td>44</td>
<td>51</td>
<td>61</td>
<td>39</td>
<td>20</td>
<td>11</td>
</tr>
<tr>
<td></td>
<td>S3</td>
<td>89</td>
<td>124</td>
<td>81</td>
<td>79</td>
<td>72</td>
<td>78</td>
</tr>
<tr>
<td><strong>Avg.</strong></td>
<td></td>
<td><strong>85</strong></td>
<td><strong>108</strong></td>
<td><strong>83</strong></td>
<td><strong>56</strong></td>
<td><strong>46</strong></td>
<td><strong>38</strong></td>
</tr>
<tr>
<td>Vastus medialis</td>
<td>S1</td>
<td>87</td>
<td>124</td>
<td>111</td>
<td>50</td>
<td>46</td>
<td>14</td>
</tr>
<tr>
<td></td>
<td>S2</td>
<td>98</td>
<td>117</td>
<td>135</td>
<td>78</td>
<td>38</td>
<td>12</td>
</tr>
<tr>
<td></td>
<td>S3</td>
<td>112</td>
<td>129</td>
<td>101</td>
<td>98</td>
<td>88</td>
<td>89</td>
</tr>
<tr>
<td><strong>Avg.</strong></td>
<td></td>
<td><strong>99</strong></td>
<td><strong>124</strong></td>
<td><strong>116</strong></td>
<td><strong>75</strong></td>
<td><strong>54</strong></td>
<td><strong>38</strong></td>
</tr>
<tr>
<td>Knee extensors</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Biceps femoris</td>
<td>S1</td>
<td>23</td>
<td>25</td>
<td>23</td>
<td>63</td>
<td>43</td>
<td>57</td>
</tr>
<tr>
<td></td>
<td>S2</td>
<td>13</td>
<td>20</td>
<td>18</td>
<td>13</td>
<td>16</td>
<td>20</td>
</tr>
<tr>
<td></td>
<td>S3</td>
<td>20</td>
<td>25</td>
<td>32</td>
<td>37</td>
<td>37</td>
<td>55</td>
</tr>
<tr>
<td><strong>Avg.</strong></td>
<td></td>
<td><strong>19</strong></td>
<td><strong>23</strong></td>
<td><strong>24</strong></td>
<td><strong>38</strong></td>
<td><strong>32</strong></td>
<td><strong>44</strong></td>
</tr>
<tr>
<td>Semitendinosus</td>
<td>S1</td>
<td>13</td>
<td>14</td>
<td>11</td>
<td>20</td>
<td>15</td>
<td>18</td>
</tr>
<tr>
<td></td>
<td>S2</td>
<td>14</td>
<td>19</td>
<td>19</td>
<td>14</td>
<td>14</td>
<td>15</td>
</tr>
<tr>
<td></td>
<td>S3</td>
<td>15</td>
<td>14</td>
<td>30</td>
<td>31</td>
<td>24</td>
<td>36</td>
</tr>
<tr>
<td><strong>Avg.</strong></td>
<td></td>
<td><strong>14</strong></td>
<td><strong>16</strong></td>
<td><strong>20</strong></td>
<td><strong>22</strong></td>
<td><strong>18</strong></td>
<td><strong>23</strong></td>
</tr>
<tr>
<td>Knee flexors</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Unit (μV); WO (without exo); Off (power off); 0% (zero torque); 10% (10% assistance); 30% (30% assistance); 50% (50% assistance).
In summary, experimental results indicate that the proposed exoskeleton is highly backdrivable with minute mechanical resistance and that moderate levels of assistance can effectively reduce muscle effort during squatting. In particular, it was observed that the proposed exoskeleton can reduce the knee extensors activity, but it is still not clear if the work is globally alleviated or simply transferred to adjacent muscle groups (e.g., hip extensors, hip flexors, ankle extensors, and ankle flexors), due to the complex mechanism of muscle group compensation. Metabolics measurements will be used in the future to perform a more in-depth analysis of the actual efficacy.

1.3.3 Back exoskeleton

Back injuries are the most prevalent work-related musculoskeletal disorders [55]. Wearable robots present an attractive solution to mitigate ergonomic risk factors and reduce musculoskeletal loading for workers who perform lifting. Over the last two decades, various studies have demonstrated that industrial exoskeletons can decrease total work, fatigue, and load while increasing productivity and work quality [1,56]. For instance, Toxiri et al. developed a powered back-support exoskeleton that reduced 30% muscular activity at the lumbar spine [4], while a passive back exoskeleton with a larger range of motion of the trunk was proposed in [57]. The key challenges of back-support exoskeletons lie in the unique anatomy of the human spine, composed of 23 intervertebral discs. Therefore this structure imposes stringent requirements that necessitate new solutions for an effective human–robot interaction.

To address the aforementioned challenge, a spine-inspired continuum soft exoskeleton has been developed with the aim of reducing spine loading during stoop lifting while not limiting the natural movements. In particular, the stoop lifting induces extension and flexion of the lumbar joints with 70 degrees in the sagittal plane. Moreover, natural range of motion allows lateral flexion of 20 degrees in the frontal plane and rotation of 90 degrees in the transverse plane. Biomechanics analysis reveals that 250 N of the exoskeleton force perpendicular to the back can decrease 30% of the lumbar compression force at the lumbosacral joint (L5/S1, between fifth lumbar and first sacral) while a 15 kg load is lifted.

1.3.3.1 Design

Due to the requirement of having a system conformal to the human back anatomy and unobtrusive for the natural movements, the proposed robot
leverages a hyperredundant continuum structure that is able to continuously bend \[58,59\], as shown in Fig. 1.15A.

Additionally, Fig. 1.15B shows the overall setup, which includes a wearable structure made of shoulder and waist braces, the high torque density actuator implemented as a tethered platform, the Bowden cable transmission, and the control system. The spinal structure is a cable-driven mechanism and has a modular architecture composed of 20 segments. Each segment comprises a disc that pivots on a ball and socket joint. Thus each pair of neighboring disks forms a three-DOF spherical joint. A cable is threaded through holes at the edges of the discs, so that when the actuator pulls the cable, the discs rotate about the ball joint, acting as levers and producing assistive torque on the human. The electric motor delivers 2 Nm nominal torque at 1500 rpm nominal speed, and it is coupled to a gearbox with 36:1 gear ratio. As a result, the actuation platform can output up to 1500 N pulling force at 0.22 m/s cable translating speed. A customized load cell placed at the bottom of the spinal structure allows measurement of the cable tension. Moreover, an elastic backbone made of coiled steel tubing ensures a tight coupling of the various segments and the integration of the overall mechanism.

1.3.3.2 Modeling
A kinematics analysis is carried out to optimize the geometrical design and to characterize the range of motion of the mechanism.

![Figure 1.15](image)

**Figure 1.15** (A) The spine-inspired back exoskeleton leverages on a hyperredundant continuum mechanism. Thanks to its compliance, this wearable robot provides assistive force while being conformal to the anatomy of the human back and unobtrusive for natural motion. (B) A healthy subject wearing the back exoskeleton to perform stoop lifting of a 15 kg load. The spine continuum mechanism is powered by a tethered actuation platform via Bowden cable transmission.
The configuration of the back exoskeleton is determined by the accumulated rotations of all discs, as shown in Fig. 1.16A.

The pose of the \((i + 1)\)-th disc with respect to the \(i\)-th disc can be represented by the homogeneous transformation

\[
T_{i+1} = \text{Rot}_x(\varphi_{i+1})\text{Rot}_y(\theta_{i+1})\text{Rot}_z(\psi_{i+1})\text{Tran}(l),
\]

where \(\varphi_{i+1}, \theta_{i+1}, \psi_{i+1}\) are the rotation angles of disc \(i + 1\) with respect to disc \(i\) in the sagittal, frontal and transverse planes, respectively, and \(l = (0 \quad 0 \quad l)^T\) is the distance vector between two neighboring discs. \(\text{Rot}_x(\cdot), \text{Rot}_y(\cdot), \text{Rot}_z(\cdot)\) denote \(4 \times 4\) homogeneous transformation matrices representing rotations around \(x, y, \) and, \(z\) axes, respectively, while \(\text{Tran}(\cdot)\) is a \(4 \times 4\) homogeneous translation matrix.

By putting all of this together, the global pose transformation of the mechanism from the base to the distal disc \(n\) can be calculated by

\[
T_{\text{tot}} = T_1 T_2 \cdots T_n.
\]

From Eq. (1.28) we see that the overall range of motion is the accumulation of the ranges of motion of individual discs. The range of motion of one disc with respect to the adjacent disc depends on the geometric parameters of the disc and the spherical joint in between, as depicted in. When the disc rotates from the initial configuration represented in Fig. 1.16B to the extreme configuration due to a mechanical contact

![Figure 1.16](image)

**Figure 1.16** Kinematics analysis of the spine continuum structure. (A) The configuration of the exoskeleton is determined by the accumulated rotations of all the discs. (B) Initial configuration of two adjacent discs. (C) Extreme configuration of two adjacent discs due to a mechanical contact constraint. (D) Variation of \(\beta\) (maximal rotation angle between two neighboring discs) with respect to the geometric parameters \(r\) (radius of the disc) and \(d\) (distance between two neighboring discs). \(\beta\) affects the range of motion of the exoskeleton.
constraint, as depicted in Fig. 1.16C, the maximal rotation angle $\beta$ can be calculated by

$$\beta = \pi - 2\arcsin\left(\frac{r}{(r + (d/2))}\right). \quad (1.29)$$

where $r$ denotes the radius of the disc, $d$ is the distance between two neighboring discs, and $l$ is the distance between the centers of two neighboring spherical joints.

Accordingly, the range of motion, related to $\beta$, can be designed by adjusting the parameters $r$ and $d$. Fig. 1.16D shows the effect of these two parameters on $\beta$.

For the present design it was chosen that $r = 0.07m$ and $d = 0.00216m$ to obtain $\beta = 20$, that allows to satisfy all the motion requirements (i.e., forward flexion of 70 degrees in the sagittal plane, lateral flexion of 20 degrees in the frontal plane, and rotation of 90 degrees in the transverse plane) with a number of discs greater than 6.

Given the kinematics characterization of the robot mechanism, it is crucial to examine a biomechanics model of human—robot interaction to facilitate the development of assistive control of the soft exoskeleton.

The kinetic purpose of the back exoskeleton is to reduce the compression and shear forces between discs, which are the main causes of low back pain. Therefore a basic analytical model of the forces acting on the human spine is derived to predict the effectiveness of the exoskeleton assistance on reducing the forces in the human spine and muscles.

For the sake of simplicity, the lumbar spine is modeled as a localized joint at the lumbar—sacral interface (L5/S1). Then, consider the condition when the human is in the flexed forward position during stoop lifting, as illustrated in Fig. 1.17. The static equilibrium analysis provides the relationship between the exoskeleton assistance and the forces in the human spine:

$$F_e D_e = - F_{exo} D_{exo} + m_{load} g D_{load} + m_{body} g D_{body} \quad (1.30)$$

$$F_p = F_e + m_{body} g \cos \theta + m_{load} g \cos \theta \quad (1.31)$$

$$F_s = - F_{exo} + m_{body} g \sin \theta + m_{load} g \sin \theta \quad (1.32)$$

$F_p$, $F_s$ denote the compressive and shear forces of intervertebral discs, $F_{exo}$ is the force applied by the back exoskeleton, and $F_e$ denotes the force...
of the erector spinae muscle. \( m_{\text{body}} \) and \( m_{\text{load}} \) are the masses of the human upper body and of the load, respectively. \( D_{\text{exo}}, D_e, D_{\text{load}}, \) and \( D_{\text{body}} \) are the moment arms of the exoskeleton, erector spinae muscle, load, and upper body, respectively.

According to Eqs. (1.30)–(1.32), it can be observed that if the exoskeleton force \( F_{\text{exo}} \) increases, the erector muscle force \( F_e \), the spine compressive force \( F_p \), and the intervertebral shear force \( F_s \) decrease simultaneously, because the weights of the human and of the load are partly balanced by the assistive force of the exoskeleton.

**1.3.3.3 Control**

The control architecture, as shown in Fig. 1.18A, consists of two main layers: a high-level controller and a low-level controller.

In the high-level controller a virtual impedance model, represented in Fig. 1.18B, is used to generate the reference assistive force according to Eq. (1.33).

\[
F_r = \frac{T_r}{r_1} = \frac{1}{r_1} \left[ J_d(\ddot{\theta}_r - \ddot{\theta}_i) + B_d(\dot{\theta}_i - \dot{\theta}_r) + K_d(\theta_i - \theta_c) \right],
\]

where \( \theta_r, \dot{\theta}_r, \) and \( \ddot{\theta}_r \) denote the desired trunk angle, velocity, and acceleration, generated from a predefined desired trajectory, while \( \theta_c, \dot{\theta}_c, \) and \( \ddot{\theta}_c \)
are the actual values measured by an IMU sensor mounted on the trunk. In this case the desired trajectory is set to zero, so that virtual spring and damper are fixed to the ground.

High-level control is implemented in Matlab/Simulink Real Time and operates at 1000 Hz frequency. A PID force control is used to ensure that the cable measured force tracks the reference force $F_r$.

In the low-level controller, a DSP microcontroller (TMS320F28335, Texas Instruments, United States) is used for motor current and velocity control. It uses CAN bus communication to receive the desired velocity command $V_r$ and to send data about the actuator state. Both velocity and current controllers implement a PID algorithm to track the reference signals.

Regarding the sensing system, a data acquisition (I/O) card (ADC, PCIe-6259, National Instrument, Inc., United States) is used to acquire
cable force measurements from the loadcell mounted on the back exoskeleton, while an IMU mounted on the subject trunk transmits the trunk motion data (angle, angular velocity, and angular acceleration) via serial port (RS-232) to the target computer.

1.3.3.4 Evaluation
The exoskeleton provides assistance in stoop lifting without limiting natural motion. As shown in Fig. 1.19, the wearer is free to perform forward flexion, lateral flexion, and rotation.

Fig. 1.15B shows the setup used for the experimental evaluation of the back exoskeleton. Besides the wearable structure, it includes the Bowden cable transmission, the tethered actuation platform, and the real-time control system. Currently, a tethered actuation system is employed to perform a proof of concept trial, aimed at demonstrating the feasibility of the proposed spine design and control algorithm, thus minimizing the impact of the mass of the system. However, it is worth highlighting that the combined mass of motor and gearbox is just 0.55 kg, hence a portable version is indeed a practicable advancement already under development.

Three subjects performed 10 repetitions of 15 kg stoop lifting. Each stoop cycle took 8 s: 4 s for bending forward from stand-up posture to trunk flexion and 4 s for extending back from trunk flexion to stand-up posture. The study was approved by the City University of New York.
Institutional Review Board, and all methods were carried out in accordance with the approved study protocol.

The first test regarded the steerability evaluation of the continuum exoskeleton, that is the relation between the cable displacement and the bending angle of the back exoskeleton, defined as the angle between the end faces of the base and the top disc.

Results shown in Fig. 1.20 indicate that a cable displacement of 5.23 cm produces a bending angle of 100 degrees, which is beyond the required range of motion of 70 degrees.

Then, the tracking performance of the assistive force control is evaluated. The desired assistance is calculated according to the virtual impedance model described by

\[
F_r = 20\dot{\theta}_a + 200 \sin \theta_a,
\]

(1.34)

where the sine function in the stiffness term has the function of compensating the involved components (which are related to \(\sin \theta_a\)) of the human and load gravity terms. Fig. 1.21 illustrates the variation of the force and the trunk angle during the stoop task, as observed from a total of 30 stoop cycles executed by three different subjects.

The RMSE of force tracking is 6.63 N (3.3% of the 200 N peak force). Therefore regardless of motion variability (represented by the standard deviation of trunk angles), the implemented controller was able to successfully track the desired force with high accuracy.

Figure 1.20  Steerability sequence of the continuum exoskeleton. The bending angle is defined as the angle between the end faces of the base and the top disc. A cable displacement of 5.23 cm is sufficient to produce a bending angle of 100 degrees.
1.4 Discussion

This chapter presented the advanced QDD actuation paradigm for high-performance wearable robots. Based on an ad hoc customized motor and low ratio gear transmission it ensures great versatility thanks to high torque density (20.7 Nm/kg), high backdrivability (0.4 Nm backdrive torque in unpowered mode), and high bandwidth (62.4 Hz). These properties are well suitable for applications involving human–robot interaction. Taking advantage of these characteristics three exoskeletons have been designed to provide assistance to the hip, the knee, and the back. Their

![Figure 1.21](image)

**Figure 1.21** Assistive force tracking performance and trunk angle measurement during stoop lifting. Tests were executed by three healthy subjects and each subject performed 10 stoop cycles, for a total of 30 stoop repetitions. The mean actual assistive force (solid line) is able to accurately track the mean reference assistive force (dashed line). The shaded area identifies the variation within ±1 standard deviation. RMSE of force tracking is 6.63 N (3.3% of the 200 N peak force).
feasibility and effectiveness were experimentally tested on healthy subjects. All of them exhibited low mechanical impedance and high accuracy in assistive force tracking, being able to overcome the performance of analogous state-of-the-art devices. In particular, the bilateral hip exoskeleton achieved 0.4 Nm backdrive torque, 62.4 Hz bandwidth, and RMSE in force tracking equal to 5.4% of 20 Nm peak torque. The bilateral knee exoskeleton presented backdrive torque equal to 1.5 Nm in unpowered mode and 0.5 Nm with zero torque tracking control, while RMSE of torque tracking was 1.2% of 24 Nm peak torque. Finally, for the spine exosuit RMSE of force tracking was about 3.3% of the 200 N peak force.

In conclusion, experimental results verify that the presented actuation paradigm offers promising features to push the limits of wearable robots’ performance. QDD actuation constitutes an enabling technology that could pave the way to the development of more lightweight, more compliant, safer, and stronger exoskeletons for either rehabilitation or augmentation purposes.

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References


High-performance soft wearable robots for human augmentation and gait rehabilitation


